NUMERICAL ANALYSIS FOR MOVING BED IRON SCRAP MELTING FURNACE

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ABSTRACT

The reduction and melting of oxidized iron-scrap briquettes containing coke breeze in a moving bed reactor has been proposed from the viewpoints of energy saving, recycling and environmental protection. The aim of this study is to investigate the effect of the briquette on operation of the reduction-melting furnace. For this purpose, a total mathematical model of the reduction-melting furnace has been developed based on the rates of briquette reduction and solid iron carburization and wetted area in a trickle bed.

The numerical simulation of the reduction-melting furnace described three-phase flow phenomena with chemical reactions and phase changes; specifically, the distributions of temperature, gas concentration, reduction degree and carburization degree in the furnace were calculated. The simulation results under different operating conditions showed that stable operation is obtained with blowing of preheated air at 673K or with 8% oxygen enrichment to air and with coke ratio fixed at 530 kg/thm.

NOMENCLATURE

- \( a \) Area [m²/m³-bed] \( \Delta HF \)
- \( C_D \) Drag coefficient [-]
- \( C_p \) Specific heat [J/kg K]
- \( d \) Mean particle diameter [m]
- \( f_r \) Gasification degree of a briquette [-]
- \( F \) Volumetric momentum flux [N/m³]
- \( F_r \) Froude number \( (=G_d/\mu) \) [-]
- \( F_{r,ij} \) Radial interaction force between phases \( i \) and \( j \) [N/m²]
- \( F_{v,ij} \) Vertical interaction force between phases \( i \) and \( j \) [N/m²]
- \( g \) Gravitational force [m/s²]
- \( G \) Mass flow rate [kg/m/s]
- \( \Delta H_t \) Enthalpy change [J/kg]
- \( h \) Enthalpy [J/kg]
- \( h_{ij} \) Heat transfer coefficient between phases \( i \) and \( j \) [W/m²K]
- \( k_a \) Surface reaction rate constant \( (k=1-4) \) [m/s]
- \( k_b \) Mass transfer rate of \( n \) component [m/s]
- \( k_2 \) Reaction rate constant for reaction \( k \) [1/s]
- \( m \) Fractional mass [-]
- \( M \) Molecular weight [kg/kmol]
- \( N_c \) Dimensionless surface tension, \( N_c=(1+\cos \theta) \) [-]
- \( P \) Pressure [Pa]
- \( Pr \) Prandtl number [-]

INTRODUCTION

Briquettes of oxidized iron-scrap containing coke breeze are attracting much attention as a new raw material for ironmaking. It offers two benefits; enhancing the reduction of iron oxide and decreasing the melting temperature of burden due to carburization of iron. However, the effect of the briquette, properties and their performance in a moving coke-bed reactor is not well understood. This paper, therefore, deals with a mathematical model of a moving bed reactor for melting scrap, where the effect of the briquette containing coke breeze is assessed. The briquette and coke are charged into the furnace (see Figure
1), in which three-phase flow phenomena exists, together with phase changes and several major reactions such as combustion, reduction and carburization. The briquette moves down slowly, starts melting in a cohesive zone and trickles in the form of hot metal and molten slag in the lower part of the furnace. In contrast, cold air blusted through tuyeres flows up through packed materials. For the simulation of this reactor, three key parameters must be known; the rates of reduction and carburization, and wetted area. these were experimentally evaluated before the development of the mathematical model. Numerical simulation was finally carried out for analyzing the effect of the briquette containing coke breeze on reduction degree and temperature distributions within the reactor.

Gravitational flow of packed particles was described by the kinematic model (Nedderman and Tuzun, 1979), in which the horizontal (radial) velocity is proportional to the vertical velocity gradient in the horizontal direction \( v_r = -B(\partial u_r / \partial r) \). The value of \( B \), the kinematic constant, is an empirical coefficient (is set equal to) 2.5 times the particle diameter. By substituting this relationship into the continuity equation for packed bed of particles, an equation is derived which is similar to the diffusion equation for the vertical velocity component:

\[
\frac{\partial u_r}{\partial r} = \frac{1}{r} \frac{\partial}{\partial r} \left( r B \frac{\partial u_r}{\partial r} \right) - R_m - S_m
\]

Here, \( R_m \) is melting rate and is given by the rate of heat transfer to particles at the melting temperature.

### MATHEMATICAL MODEL

#### 1. Governing Equations

In order to estimate the effectiveness of different briquettes (e.g. carbon content), a mathematical model, which simulates all phenomena of heat transfer, fluid flow and chemical reactions, is developed. The mathematical model consists of equations for conservation of mass, momentum, thermal energy and rate equations of heat exchange, chemical reactions and scrap melting. The methodology for mathematical modeling of multiphase flows has been described in previous papers (Yagi et al., 1992a, 1992b and 1994). Based on these investigations, transport phenomena can be described by the following general equation with several assumptions, i.e. steady state continuous flow, axisymmetry and no temperature gradient within packed materials.

\[
\frac{\partial \left( \varepsilon_r \rho_r \Phi_i \right)}{\partial x} + \frac{1}{r} \frac{\partial}{\partial r} \left( r \rho_r \Phi_i \frac{\partial \Phi_i}{\partial r} \right) = \frac{\partial}{\partial x} \left( \varepsilon_r \rho_r \frac{\partial \Phi_i}{\partial x} \right) + \frac{1}{r} \frac{\partial}{\partial r} \left( r \rho_r \frac{\partial \Phi_i}{\partial r} \right) + S_i
\]

The dependent variable \( \Phi_i \), diffusive transport coefficient \( \Gamma_{\Phi_i} \) and source term \( S_i \) are described in Table 1. The source term includes interaction forces and gravity for momentum transfer, melting rate for mass transfer and heat exchange, reaction heat and melting heat for thermal energy transfer.

### Table 1: Dependent variable, diffusive transport coefficient and source term.

<table>
<thead>
<tr>
<th>( i )</th>
<th>( \Phi_i )</th>
<th>( \Gamma_{\Phi_i} )</th>
<th>( S_i )</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>( \Phi_i )</td>
<td>( \Gamma_{\Phi_i} )</td>
<td>( S_i )</td>
</tr>
<tr>
<td>g</td>
<td>1</td>
<td>0</td>
<td>( S_m )</td>
</tr>
<tr>
<td>g</td>
<td>( u_g )</td>
<td>( \mu_g )</td>
<td>( -\frac{1}{\varepsilon_g} \frac{\partial \rho_g}{\partial x} )</td>
</tr>
<tr>
<td>v</td>
<td>( v_g )</td>
<td>( \mu_g )</td>
<td>( -\frac{1}{\varepsilon_g} \frac{\partial \rho_g}{\partial r} )</td>
</tr>
<tr>
<td>h</td>
<td>( h_g )</td>
<td>( \lambda_g/C_p_g )</td>
<td>( \sum_{\text{chem}} \Phi_{g_i} (T_g - T_i) + \sum_{\text{residuals}} \Delta H_i R_t + \Delta H_m )</td>
</tr>
<tr>
<td>m</td>
<td>( m_s )</td>
<td>( \rho_s D_s )</td>
<td>( \sum_{\text{chem}} \frac{V_{g_i}}{r_s} R_t )</td>
</tr>
<tr>
<td>s</td>
<td>1</td>
<td>0</td>
<td>( -R_m - S_m )</td>
</tr>
<tr>
<td>s</td>
<td>( h_s )</td>
<td>( \lambda_s/C_p_s )</td>
<td>( \sum_{\text{chem}} \Phi_{s_i} (T_s - T_i) + \sum_{\text{residuals}} \Delta H_i R_t - \Delta H_m - \Delta H_s )</td>
</tr>
<tr>
<td>s</td>
<td>( m_{P_s} )</td>
<td>0</td>
<td>( -R_m )</td>
</tr>
<tr>
<td>t</td>
<td>1</td>
<td>0</td>
<td>( R_m )</td>
</tr>
<tr>
<td>t</td>
<td>( u_t )</td>
<td>( \mu_t )</td>
<td>( -\varepsilon_t \rho_t g + F_{s_i} g_l - F_{s_i} t_s )</td>
</tr>
<tr>
<td>t</td>
<td>( v_t )</td>
<td>( \mu_t )</td>
<td>( F_{s_i} g</td>
</tr>
<tr>
<td>h</td>
<td>( h_t )</td>
<td>( \lambda_t/C_p_t )</td>
<td>( \sum_{\text{chem}} \Phi_{t_i} (T_t - T_i) + \Delta H_m )</td>
</tr>
</tbody>
</table>

### Coke and Gas Phase Reactions

In the reactions of coke combustion and coke gasification, the total reaction rates, including chemical reaction and gas laminar film diffusion, were applied (Muchi et al., 1966, Field et al., 1967, Heynert et al., 1959). Here, the reaction rate of complete combustion of \( C \) and \( O_2 \) is
evaluated using the ratio between CO$_2$ and CO (Arthur, 1951).

$$R_k = \frac{a_k}{k_{ii}^2 + k_{ij}^2} \frac{12 \rho \epsilon_{gs}}{M_n}$$  \hspace{1cm} (3)

$$R_2 : \frac{C_1}{C_2} = 2500 \exp(-6240 / T_e)$$  \hspace{1cm} (4)

In the combustion reaction of CO, the Howard’s equation (1973) was employed.

$$R_g = 3.64 \times 10^{-11} \epsilon_0 C_{Fe}^{1/4} C_{O}^{1/5} \exp(-15106 / T_e)$$  \hspace{1cm} (5)

We assumed that the water gas shift reaction and combustion of H$_2$ were equilibrium reactions.

<table>
<thead>
<tr>
<th>Reaction</th>
<th>No.</th>
</tr>
</thead>
<tbody>
<tr>
<td>Combustion and gasification of coke</td>
<td>1</td>
</tr>
<tr>
<td>C + O$_2$ = CO</td>
<td>2</td>
</tr>
<tr>
<td>C + CO$_2$ = 2CO</td>
<td>3</td>
</tr>
<tr>
<td>C + H$_2$O = CO + H$_2$</td>
<td>4</td>
</tr>
<tr>
<td>Gaseous</td>
<td>5</td>
</tr>
<tr>
<td>CO + 1/2 O$_2$ = CO$_2$</td>
<td>6</td>
</tr>
<tr>
<td>CO + H$_2$O = CO$_2$ + H$_2$</td>
<td>7</td>
</tr>
<tr>
<td>Reduction</td>
<td>8</td>
</tr>
<tr>
<td>Fe$<em>{O}$O$</em>{Fe} + (2\times x)\ CO + (m-x)\ CO$_2$</td>
<td></td>
</tr>
<tr>
<td>Carburization</td>
<td>9</td>
</tr>
<tr>
<td>2CO = C$_{inFe}$ + CO$_2$</td>
<td>10</td>
</tr>
</tbody>
</table>

Table 2: Reactions in the reduction-melting furnace.

Reactions of Briquette

Two kinds of briquette having different amounts of coke breeze were used in the numerical simulation. These are described in Table 3.

<table>
<thead>
<tr>
<th>Briquette</th>
<th>T.Fe</th>
<th>M.Fe</th>
<th>Fe$^{2+}$</th>
<th>Fe$^{3+}$</th>
<th>O</th>
<th>C</th>
<th>C/O</th>
</tr>
</thead>
<tbody>
<tr>
<td>B1</td>
<td>70.0</td>
<td>17.1</td>
<td>43.5</td>
<td>9.4</td>
<td>16.4</td>
<td>7.4</td>
<td>0.60</td>
</tr>
<tr>
<td>B2</td>
<td>67.0</td>
<td>17.7</td>
<td>42.3</td>
<td>7.0</td>
<td>15.1</td>
<td>11.2</td>
<td>0.99</td>
</tr>
</tbody>
</table>

Table 3: Chemical composition of briquettes (mass%).

Reaction rates for the reduction of iron oxide, the gasification of coke and the thermal decomposition of the binder in the oxidized iron-scrap briquette containing coke breeze were utilized. The reaction of a single briquette was studied experimentally by measuring changes of weight and gas volume at fixed temperature in a nitrogen atmosphere (Zhang et al., 1995). The result was that reaction of the briquette is coincident with reactions of gasification of coke by CO$_2$ gas and reduction of iron oxide by CO gas. The reduction of iron oxide is in an equilibrium step and the gasification reaction is a rate-limiting step. It was, therefore, concluded that the reduction rate of iron oxide is evaluated from the gasification rate shown below.

$$R_k = k_{3} m_{Fe} \rho_{Fe} \epsilon_{k}$$  \hspace{1cm} (6)

For B1 briquette:  \( \epsilon'_{s} = 1 - \exp(6.91 - 0.00568 T_e) \)

$$k_s = \begin{cases} 
99.12 \exp(-138 \times 10^7 / RT) & (\epsilon'_{s} \leq \epsilon'_{s}) \\
3.663 \exp(-116 \times 10^7 / RT) & (\epsilon'_{s} > \epsilon'_{s}) 
\end{cases}$$  \hspace{1cm} (7)

For B2 briquette:  \( \epsilon'_{s} = 1 - \exp(8.18 - 0.00675 T_e) \)

$$k_s = \begin{cases} 
27.94 \exp(-123 \times 10^7 / RT) & (\epsilon'_{s} \leq \epsilon'_{s}) \\
2.24 \exp(6.8 \times 10^7 / RT) & (\epsilon'_{s} > \epsilon'_{s}) 
\end{cases}$$  \hspace{1cm} (8)

Carburization Rate

The carburization rate of solid iron by CO was obtained by thermo-gravimetrical analysis. The diffusion coefficient of carbon in solid iron was also obtained from the carbon content distribution in solid iron by EPMA analysis (Zhang et. al., 1997).

The carburization mechanism can be described as a two step process of surface carburization and diffusion of carbon into solid iron. The surface carburization reaction proceeds via two elemental reactions, as described below;

\[ \text{CO} = \text{O} \text{(ads)} + \text{C} \text{(in Fe)} \]
\[ \text{O} \text{(ads)} + \text{CO} = \text{CO}_2 \]

Here, dissociation of CO is in equilibrium and elimination of O adsorbed is rate-determining step. As a result, the reaction rate can be expressed below.

$$R_s = k_8 \frac{K_p \rho_{CO} \epsilon^s_{Fe} - k_9 \rho_{CO} \epsilon^s_{Fe} \exp(a c \rho_{CO})}{K_p \rho_{CO} \epsilon^s_{Fe} + K_p \rho_{CO} \epsilon^s_{Fe} \exp(a c \rho_{CO})}$$  \hspace{1cm} (9)

Iron Melting Rate

The iron melting rate was calculated using equation (8) which was based on the assumption of the heat transfer being rate-limiting.

$$R_m = a_{Fe} h_{gs} (T_e - T_m) / \Delta H_m$$  \hspace{1cm} (10)

The melting point, \( T_m \), was regarded as the surface melting temperature of iron. It was measured using a hot-stage microscope.

3. Parameter Evaluation

Before carrying out a numerical analysis using the mathematical model, unknown parameters, such as contact area, exchange of momentum and heat transfer between heterogeneous phases, must be formulated.

Contact Area between Heterogeneous Phase

Obviously, liquid generation decreases both voidage and the contact area between gas and solid in the reduction-melting furnace. We assumed in this mathematical model that the dynamic hold-up of the liquid was assumed to be volumetric fraction of the liquid.

$$\epsilon_{g} + \epsilon_{s} + \epsilon_{l} = 1$$  \hspace{1cm} (11)
\( a_{g} \) is the contact area between gas and liquid obtained by using Mada’s equation (Mada, 1963), and \( a_{s} \) the contact area between liquid and solid obtained by using Niu’s equation (Niu et al., 1996), which is the equation modified from Onda’s equation (Onda et al., 1967). \( a_{gs} \) is the contact area between gas and solid calculated as the difference in surface area of solid and contact area between liquid and solid. They can be expressed as following equations.

\[
\begin{align*}
\dot{a}_{g} &= 0.34 \beta_{F}^{-2/3} W_{e}^{2/3} / d_{s} \\
\dot{a}_{l} &= \frac{6g}{d_{s}} \left( 0.4 \left( Re_{g} / e_{g} \right) ^{0.218} W_{e}^{0.0423} \right) N_{c}^{-0.0235} \\
\dot{a}_{s} &= 6 \sigma_{r} / d_{s} \cdot \dot{a}_{s}
\end{align*}
\] (10)

**Exchange of the Momentum**

The interaction force between gas and solid was evaluated using Ergun’s equation developed by considering the liquid-gas interaction. It is described by equation (13).

\[
\vec{F}_{g} = \left[ \frac{150 \mu_{ls} \alpha_{g}}{38(1-\varepsilon_{f})} + \frac{175 \mu_{ls} \alpha_{g}}{6} \right] \frac{\left| \vec{v}_{g} - \vec{v}_{s} \right|}{(\vec{v}_{g} - \vec{v}_{s})}
\] (13)

The interaction force between dripping liquid and rising gas through pore space in the packed bed was evaluated using Fanning’s equation. This was developed by considering both the flows of gas and liquid in the packed bed and the contact area between gas and liquid. It is represented as equation (14).

\[
\vec{F}_{g} = \frac{\dot{a}_{g}}{\dot{a}_{s} + \dot{a}_{s}} \left( \frac{3C_{p} \rho_{e}}{4d_{s}} \right) \left( \vec{v}_{g} - \vec{v}_{s} \right)
\] (14)

The interaction force between liquid and solid in the reduction-melting furnace was evaluated by the Kozeny-Carman equation developed using the contact area between liquid and solid. It is given as equation (15).

\[
\vec{F}_{s} = \frac{180 \mu_{ls} \alpha_{g}}{38(1-\varepsilon_{f})} \left( \vec{v}_{g} - \vec{v}_{s} \right)
\] (15)

**Heat Transfer**

The heat transfer coefficients between gas and solid and between gas and liquid represented as equation (16, 17) were evaluated using the Ranz-Marshall equation as modified by Akiyama et al. (1990). The heat transfer coefficient between liquid and solids was evaluated by the equation (18), which is for forced convection heat transfer proposed by Pohlhausen (1921).

\[
\begin{align*}
\dot{h}_{g} &= 2.0 + 0.39 Re_{g}^{1/2} Pr_{g}^{1/3} \lambda_{g} / d_{s} \\
\dot{h}_{l} &= 2.0 + 0.39 Re_{g}^{1/2} Pr_{g}^{1/3} \lambda_{g} / d_{s} \\
\dot{h}_{s} &= 0.664 Re_{g}^{1/2} Pr_{g}^{1/3} \lambda_{g} / d_{s}
\end{align*}
\] (16)

**4. Experimental Verification**

Before numerical simulations of the moving bed reactor were conducted, the mathematical model, together with rate parameters summarized above, were experimentally verified using a laboratory-scale combustion furnace of a coke bed. Figure 2 shows the comparison observed between calculated and measured distributions of temperature and gas composition within the furnace. The good agreement provides support for the underlying assumptions made in the model.
supplied at the furnace top, and the temperature and the coke ratio were fixed as constant values. Regarding the liquid phase, it is formed in the melting zone and continuously discharged from the furnace bottom.

**Operating Conditions**

The temperature and physical properties of charged burden materials for the numerical simulation of briquette melting process are given in Table 4.

<table>
<thead>
<tr>
<th>Material</th>
<th>Temp. (K)</th>
<th>Diameter (mm)</th>
<th>Porosity (-)</th>
<th>Density (kg/m³)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Coke</td>
<td>298</td>
<td>50</td>
<td>0.52</td>
<td>1000</td>
</tr>
<tr>
<td>Briquette</td>
<td>298</td>
<td>35</td>
<td>0.48</td>
<td>3280</td>
</tr>
</tbody>
</table>

**Table 4**: Operating conditions for briquette melting process.

2. Results and Discussion

**Reduction Degree of Briquette**

Figure 4 shows the distributions of reduction degree of the briquettes, B1 and B2 under the condition of blowing preheated air at 673K. Significant differences in the results showed that the final reduction degree for the operation with briquette B2 was 30% higher than that with briquette B1. The high reduction degree of briquette B2 was caused by a high coke breeze content in the briquette. This clearly demonstrated the enhancement in reduction rate of briquette with increasing carbon content.

**Condition in Stable Operation**

The briquette reduction-melting process was analyzed numerically by changing the air preheating temperature (313 ~ 873 K) and oxygen enrichment (0 ~ 14%), when charging briquette B2 and keeping coke ratio at 530 kg/thm. According to the numerical results, the briquette was not well melted due to the shortage of high temperature heat in the lower part of the furnace when the blast is not preheated to over 600K, or the oxygen enrichment is below 6% in the case of an ambient temperature blast.

Figure 5 shows numerical simulations of temperature distributions of gas, solid and liquid in the reduction-melting furnace when charging briquette B2 and keeping coke ratio fixed at 530 kg/thm. Case (a) is with air preheated at 673K but no oxygen enrichment, and Case (b) is with 8% oxygen enrichment to air with out preheating.

**Gas Composition Distribution**

Figure 6 shows distributions of gas composition under the conditions of charging briquette B2 and blowing preheated air at 673K. In the region very close to the tuyere, oxygen was quickly consumed through coke combustion. The subsequent consumption of carbon dioxide by the Boudouard reaction led to a significant decrease in its concentration in the radial direction.
Correspondingly, the concentration of carbon monoxide increased in the direction away from the tuyere. The utilization factor of carbon monoxide was low due to the use of small particle coke. The carbon monoxide should be recycled.

The numerical simulation describes three-phase flow phenomena, with chemical reactions and phase changes. The distributions of temperature, gas concentration, reduction degree and carburization degree in the reduction-melting furnace are calculated. The reduction degree distribution showed that the charging of briquette B2 was better than the charging of briquette B1. This was due to a higher content of coke breeze in briquette B2 than briquette B1. Simulation results for different operating conditions showed that stable melting of the oxidized iron-scrap briquette was obtained under preheated air blowing at 673K or with 8% oxygen enrichment to air blowing in the case of coke ratio fixed at 530 kg/thm.

REFERENCES


POHLHAUSEN, E., (1921), Z. Angew. Math & Mech., 1, 115 - 121.


